**10.1 Study Guide and Intervention**

***Geometric Mean***

**Geometric Mean** The **geometric mean** between two numbers is the positive square root of their product.   
For two positive numbers *a* and *b*, the geometric mean of *a* and *b* is the positive number *x* in the proportion = .   
Cross multiplying gives = *ab*, so *x* = *.*

**Example : Find the geometric mean between each pair of numbers.**

**a. 12 and 3**

*x* = Definition of geometric mean

= *a* = 12 and *b* = 3

= Factor.

= 6 Simplify.

The geometric mean between 12 and 3 is 6.

**b. 8 and 4**

*x* = Definition of geometric mean

= *a* = 8 and *b* = 4

= Factor.

= Associative Property

= 4 Simplify.

The geometric mean between 8 and 4 is 4 or about 5.7.

**Exercises**

**Find the geometric mean between each pair of numbers.**

**1.** 4 and 4 **2.** 4 and 6

**3.** 6 and 9 **4.**  and 2

**5.** 12 and 20 **6.** 4 and 25

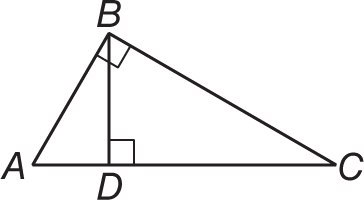
**7.** 16 and 30 **8.** 10 and 100

**9.**  and **10.** 17 and 3

**11.** 4 and 16 **12.** 3 and 24

**10.1 Study Guide and Intervention** *(continued)*

***Geometric Mean***

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**Geometric Means in Right Triangles** In the diagram, △*ABC* ∼ △*ADB* ∼ △*BDC*.   
An altitude to the hypotenuse of a right triangle forms two right triangles. The two triangles are similar and each is similar to the original triangle.

**Example 1: Use right △ *ABC* with ⊥ . Describe two geometric means.**

**a.** △*ADB* ∼ △*BDC* so = .

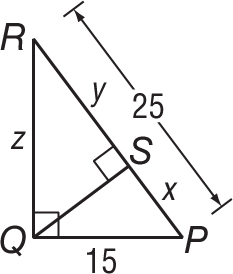
In △*ABC*, the altitude is the geometric mean between the two segments of the hypotenuse.

**b.** △ABC ∼ △*ADB* and △*ABC* ∼ △*BDC*,

so = and = .

In △ *ABC*, each leg is the geometric mean between the hypotenuse and the segment of the hypotenuse adjacent to that leg.

**Example 2: Find *x*, *y*, and *z*.**

 15 = Geometric Mean (Leg) Theorem

15 =  *RP* = 25 and *SP* = *x*

225 = 25*x* Square each side.

9 = *x* Divide each side by 25.

Then

*y* = *RP* – *SP*

= 25 – 9

= 16

*z* = Geometric Mean (Leg) Theorem

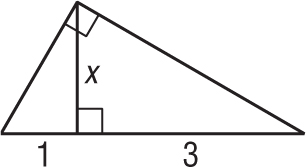
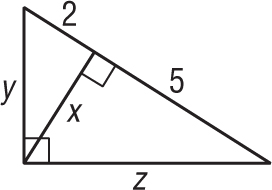
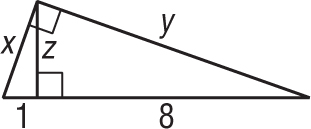
= *RS* = 16 and *RP* = 25

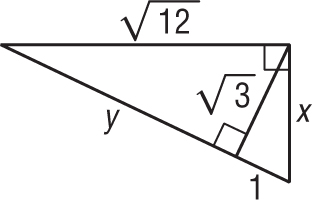
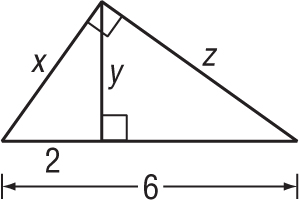
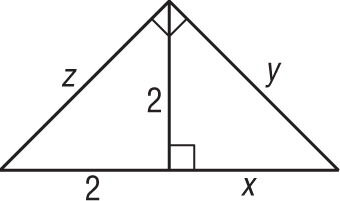
= Multiply.

= 20 Simplify.

**Exercises**

**Find *x*, *y*, and *z* to the nearest tenth.**

**1. 2. 3.**

** 4. 5. 6.**